

Study on Anti Topological Ordered Spaces

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Abstract: In the exploration of topological spaces across various contexts, the cornerstone concepts revolve around open sets, closed sets, as well as the notions of interior and exterior of a set. Equivalently fundamental are the foundational principles encountered when delving into the realm of Anti-topological spaces (ATS). The landscape of mathematical inquiry delves into the intricate definitions and properties of anti-open sets, anti-closed sets, anti-interiors, anti-exterior, as well as b-anti-open sets, b-anti-closed sets, anti-b-interiors, and anti-b-closures, among a rich array of others. Scholars worldwide have not only encountered but also delved deep into these foundational ideas. This article introduces, studies, and analyzes fundamental properties of concepts like Anti-g-closed, Anti-g-open, Anti-ig-closed, Anti-dg-closed, and Anti-bg-closed specifically within the context of "Anti-topological ordered spaces (ATOS)".

Keywords: Anti-g-closed (Anti-g-c), Anti-g-open (Anti-g-o), Anti-ig-closed (Anti-ig-c), Anti-dg-closed (Anti-dg-c) and Anti-bg-closed (Anti-bg-c).

1. Introduction

In 2021, Şahin et al. introduced the concept of ATS, a significant milestone in mathematical exploration. This ground breaking work inspired further investigation, including Witczak's comprehensive study. Within this work, Witczak delved into anti-interior and anti-closure for sets, analyzing their properties in depth. The study also explored anti-dense sets and anti-nowhere-dense sets, shedding light on their essential characteristics. Additionally, the concept of anti-continuity was examined, contributing to the evolving discourse in this field.

Over the years, researchers have extensively explored open and closed sets [1, 2, 3, 4, 9, 13, 14, 16, 17] across various mathematical contexts. Witczak [29] expanded on this research thread by introducing concepts like anti-semi-open sets, pseudo-anti-open sets, and anti-genuine sets. Recently, Khaklary and Ray [11] contributed to this body of work by introducing and investigating a diverse array of open sets in the context of anti-topological spaces. These included anti-p-oss, anti-p-css, r-oss, r-css, α -oss, α -css, & more, thus enriching our understanding of topological structures with anti-properties.

This article contributes to the advancement of the field by unveiling innovative concepts within Anti-Topological spaces. Specifically, we introduce the novel notions of Anti-g-open sets and Anti-g-closed sets, enriching our understanding of these spaces. Additionally, we explore the realms of ATOS by defining Anti-ig-c, Anti-dg-c, and Anti-bg-c sets, offering fresh perspectives & insights into the intricacies of these ordered spaces.

2. preliminaries

Definition 2.1[38]: In the background of a non-empty set X and its associated clan τ of subsets, we can define an Anti-topological space (X, τ) , where τ is referred to as the Anti-topology. In this framework, τ must fulfil any of the subsequent criteria {i, ii, iii} to qualify as an Anti-topology.

(i) $\emptyset, X \notin \tau$

(ii) For each n which is finite with $s_1, s_2, s_3, \dots, s_n \in \tau, \bigcap_{i=1}^n s_i \notin \tau$.

(iii) For each set $s_1, s_2, s_3, \dots, s_n \in \tau, \bigcup_{i \in I} s_i \notin \tau$, in which I is a reference set.

Anti-Closed sets can be understood as the complements of Anti-Open sets within the context of an anti-topological space. These Anti-oss

represent the counterpart of traditional o-ss in the context of ATS.

Remark 2.2[38]: In a space devoid of topology. It is satisfied that beneath are met.

(i) X and the empty set are not Anti-o.

(ii) It is not Anti-o to join the Anti-oss.

(iii) It is not Anti-o when the Anti-oss intersect.

Definition 2.3[38]: The collection comprising all Anti-Open portions of a set 'A' is its Anti-Interior in an ATS (X, τ) . Declared otherwise, Anti-int(A) refers to the combine to all sets B, where B is a portion of A and B is Anti-Open.

Definition 2.4[38]: The meeting of all Anti-Closed the extra sets of a set 'A' are referred to as the Anti-Closure of the set A that occurs in Anti-topological space (X, τ) . To say it another way, Anti-cl(A) is the meet of all sets G, where G is Anti-Closed and an extra set of A.

Lemma 2.5[38]: Suppose that $A \subseteq B$, $B \in \tau$, and (X, τ) is an ATS. After that, $A \notin \tau$.

Proof: If " $A \subseteq B$ then $A = A \cap B$ " and " $A \cap B \notin \tau$ ".

Lemma 2.6[38]: Let X be a dimension that isn't empty. Let U be an assortment of X portions that, if merged arbitrarily, are anti-closed. When there are finite intersections, it is then anti-closed.

Proof: Pretend as " A and B " are both independent parts of ' X ' which means " $A, B \in U$ & $A \cap B \in U$ ". Finally, acknowledge that " $A \cup (A \cap B) = A$ ". Due to agreements prohibit closure, $A \notin U$. This is incoherent. Keep in mind that under finite unions, assuming Anti-closure was sufficient. A few characteristics of Anti-css can be examined.

Lemma 2.7[38]: Infer that $A, B \in \tau_{cl}$ while (X, τ) is an ATS. Believe " $A \neq B$ ". Next, " $A \cap B \notin \tau_{cl}$ ".

Proof: If $A, B \in \tau_{cl}$ indicates that $-A, -B \in \tau$. Let $A \cap B \in \tau_{cl}$. At that, $-(A \cap B) \in \tau$. Fortunately $-A \cup -B \in \tau$, and this is in disagreement.

Lemma 2.8[38]: Infer that $\{A_i\}_{i \in J} \subseteq \tau_{cl}$ as well as (X, τ) is an ATS. Later that, $\bigcup_{i \in J} A_i \notin \tau_{cl}$.

Proof: Let $\bigcup_{i \in J} A_i \in \tau_{cl}$. As a result, (by reason of De Morgan's rules) $\bigcap_{i \in J} (-A_i) \in \tau$. Consequently,

$-\bigcup_{i \in J} A_i \in \tau$. Fortunately $A_i \in \tau$ applies to all $i \in J$, consequently their meeting should be exceeding τ . This is incoherent.

Definition 2.9[38]: If A is an Anti-PreOpen set if and solely if $A \subseteq (AntiCl(A))$ and (X, τ) is an ATS and $A \subseteq X$.

Definition 2.10[38]: If (X, τ) is an ATS and accepting " $A \subseteq X$ " & A is an anti-SemiOpen set, then A are likely to be such if $A \subseteq (Ant(A))$.

Definition 2.11[15]: If $A \subseteq AntiInt(AntiCl(AntiInt(A)))$ and (X, τ) is an ATS with $A \subseteq X$, then A is Anti-AlphaOpen.

Definition 2.12[15]: A is considered Anti-RegularOpen if and only if $A = AntiInt(AntiCl(A))$, where $A \subseteq X$ and (X, τ) is an ATS.

Definition 2.13[15]: A is designated as Anti-BetaOpen if $A \subseteq (Ant(AntiCl(A)))$. This is assuming that (X, τ) is an ATS and $A \subseteq X$.

Definition 2.14[15]: If portion A of an ATS (X, τ) is Anti-RegularOpen in X , or equivalently, if $A = AntiCl(AntiInt(A))$, then A^c is Anti-RegularClosed in X .

Definition 2.15[15]: Anti-AlphaClosed is a portion A of an ATS (X, τ) if $AntiCl(AntiInt(AntiCl(A))) \subseteq A$.

Definition 2.16[15]: If $AntiInt(Ant(A)) \subseteq A$, then a portion A of an ATS (X, τ) is considered anti-semiclosed.

Definition 2.17[15]: If $AntiCl(AntiInt(A)) \subseteq A$, then a portion A of an ATS (X, τ) is "AntiPreClosed".

Definition 2.18[15]: If A is "AntiBetaClosed" if $AntiInt(AntiCl(AntiInt(A))) \subseteq A$ and X is an anti-topological space and $A \subseteq X$.

Definition 2.19[15]: If a portion of an ATS (X, τ) is both anti-o & anti-closed, it is referred to as anti-clopen.

3. Anti-g-closed sets

Definition 3.1: If $A \subseteq O$ and O is Anti-open, then A is Anti-g-c iff $Anti-cl(A) \subseteq O$.

Theorem 3.2: If $Anti-cl(A)-A$ fails to include any non void Anti-closed sets, iff A is Anti-g-c.

Proof: Suppose that F represents an Anti-closed subset of $Anti-cl(A)-A$. Since A is anti-g-c, we get $Anti-cl(A) \subseteq C(F)$ or $F \subseteq C(Anti-cl(A))$. Thus, $A \subseteq C(F)$. $F \subseteq Anti-cl(A) \cap C(Anti-cl(A)) = \emptyset \Rightarrow F = \emptyset$. Contrariwise, pretend that $A \subseteq O$ & O is Anti-o. $Anti-cl(A) \cap C(O)$ is a non-void Anti-c portion of $Anti-cl(A)-A$ if $cl(A)$ does not include O .

Theorem 3.3: Given two sets of anti-g-css, $A \cap B$ is also Anti-g-c.

Proof: If " $A \cap B \subseteq O$ & O is Anti-open", $\text{Anti-cl}(A) \subseteq O$ and $\text{Anti-cl}(B) \subseteq O$. $\text{Anti-cl}(A) \cap \text{Anti-cl}(B) \subseteq O \cap O = O \Rightarrow \text{Anti-cl}(A) \cap \text{Anti-cl}(B) \subseteq O$ (1)

W.k.t $\text{Anti-cl}(A \cap B) \subseteq \text{Anti-cl}(A) \cap \text{Anti-cl}(B)$ (2)

From (1) & (2), we get " $\text{Anti-cl}(A \cap B) \subseteq \text{Anti-cl}(A) \cap \text{Anti-cl}(B) \subseteq O$ ".

$\text{Anti-cl}(A \cap B) \subseteq O$

Therefore $\text{Anti-cl}(A \cap B) \subseteq O$ whenever $A \cap B \subseteq O$ & O is Anti-open.

Hence $A \cap B$ is Anti-g-c.

Theorem 3.4: Assume that B is an Anti-g-cs with respect to A & A is an Anti-g-c portion of X . In X , B is resulting in Anti-g-c.

Proof: Let $B \subseteq O$ & O be Anti-o in X . Then " $B \subseteq A \cap O$ " & hence $\text{Anti-cl}_A(B) = A \cap O$. Thus, it concludes that $A \cap \text{Anti-cl}(B) \subseteq A \cap O$ and $A \subseteq O \cup C(\text{Anti-cl}(B))$. Because A is Anti-g-c in X , we get $\text{Anti-cl}(A) \subseteq O \cup C(\text{Anti-cl}(B))$. Which means $\text{Anti-cl}(B) \subseteq \text{Anti-cl}(A) \subseteq O \cup C(\text{cl}(B)) \Rightarrow \text{Anti-cl}(B) \subseteq O$.

Theorem 3.5: If A is Anti-g-c & $A \subseteq B \subseteq \text{Anti-cl}(A)$, then B is Anti-g-c.

Proof: $\text{Anti-cl}(B) \cap B \subseteq \text{Anti-cl}(A) \cap A$ & because $\text{Anti-cl}(A) \cap A$ lacks a known theorem, neither does $\text{Anti-cl}(B) \cap B$ have any non-empty Anti-closed subsets.

Theorem 3.6: Presume that A is anti-g-closed in X & let " $A \subseteq Y \subseteq X$ ". In regard to Y , A is consequently Anti-g-c.

Proof: Let $A \subseteq Y \cap O$ & O be Anti-open in X . Then $A \subseteq O$ & Consequently, " $\text{Anti-cl}(A) \subseteq O$. $Y \cap \text{Anti-cl}(A) \subseteq Y \cap O$ " is the consequent relationship.

4. Anti-g-open

Definition 4.1: A is anti-generalized open if $C(A)$ is anti-g-c.

Theorem 4.2: If A is Anti-g-o, iff $F \subseteq \text{Anti-int}A$ when F is Anti-c & $F \subseteq A$.

The easy proof is left to the reader.

Theorem 4.3: The set $A \cup B$ is Anti-g-open if A and B are distinct.

Proof: Set F to be an anti-c portion of $A \cup B$. $F \cap \text{Anti-cl}(A) \subseteq A$ & consequently, by established

theory $F \cap \text{Anti-cl}(A) \subseteq \text{Anti-int}(A)$. Ily, $F \cap \text{Anti-cl}(B) \subseteq \text{Anti-int}(B)$. Now $F = F \cap (A \cup B) \subseteq (F \cap \text{Anti-cl}(A)) \cap (F \cap \text{Anti-cl}(B)) \subseteq \text{Anti-int}A \cup \text{Anti-int}B \subseteq \text{Anti-int}(A \cup B)$. Hence $F \subseteq \text{Anti-int}(A \cup B)$ & by established theory $A \cup B$ is Anti-g-open. Since $F \subseteq \text{Anti-int}(A \cup B)$, $A \cup B$ is Anti-g-o by theorem.

Corollary 4.4: Let A and B be Anti-g-css with separated $C(A)$ and $C(B)$. Next $A \cap B$ is Anti-g-c.

The demonstration derives immediately from theorem by proving that $C(A \cap B)$ is Anti-g-o.

Theorem 4.5: A set A is Anti-g-o in (X, τ) iff $O = X$ every time O is Anti-o & $\text{Anti-int}A \cup C(A) \subseteq O$.

Proof: Suppose that O is Anti-open & $\text{Anti-int}A \subseteq O$. Now $C(O) \subseteq \text{Anti-cl}(C(A)) \cap A = \text{Anti-cl}(C(A)) - C(A)$. Because $C(O)$ is Anti-c and $C(A)$ is Anti-g-c, by established theory it follows that $C(O) = \emptyset$ or $X = O$. Conversely presume that F is an Anti-cs and $F \subseteq A$. From established theory, it works to establish that $F \subseteq \text{Anti-int}A$. Now $\text{Anti-int}A \cup C(A) \subseteq \text{Anti-int}A \cup C(F)$ and hence $\text{Anti-int}A \cup C(F) = X$. It means consequently that $F \subseteq \text{Anti-int}A$.

Theorem 4.6: If " $A \subseteq B \subseteq X$ " whereby A is Anti-g-o with regard to B & B is Anti-g-o with regard to X , then A is Anti-g-o corresponding to X .

Proof: Let F be an Anti-cs and presume that $F \subseteq A$. Consequently, $F \subseteq \text{Anti-int}_B A$ since F is anti-closed with respect to B . Thus there's an Anti-open set O to ensure $F \subseteq O \cap B \subseteq A$. But $F \subseteq O^* \subseteq B$ for some Anti-oss O^* since B is Anti-g-o in X . Thus $F \subseteq O^* \cap O \subseteq B \cap O \subseteq A$. It emerges thus that $F \subseteq \text{Anti-int}A$. Using theorem A is Anti-g-o in X .

Theorem 4.7: If $\text{Anti-int}A \subseteq B \subseteq A$ & A is Anti-g-o, then B is Anti-g-o.

Proof: $C(A) \subseteq C(B) \subseteq \text{Anti-cl}(C(A))$ and since $C(A)$ is Anti-g-c, it argues that $C(B)$ is Anti-g-c by argument hence B is Anti-g-o.

5. Anti-ig, dg and bg css in ATOS

Definition 5.1: "If (X, \leq) is a partially ordered set and (X, τ) is an anti-topological space, the triplet (X, τ, \leq) happens to be anti-topological ordered space".

Definition 5.2: The notation $[x, \rightarrow]$ will represent $\{y \in X/x \leq y\}$ for each $x \in X$. If $A = \text{Anti-i}(A)$, where $\text{Anti-i}(A) = \bigcup_{x \in A} [x, \rightarrow]$, then portion A of an ATOS (X, τ, \leq) is anti-increasing.

Definition 5.3: The notation $[\leftarrow, x]$ will represent $\{y \in X/y \leq x\}$ for each $x \in X$. If $A = \text{Anti-d}(A)$, where $\text{Anti-d}(A) = \bigcup_{x \in A} [\leftarrow, x]$, then portion A of an ATOS (X, τ, \leq) is anti-decreasing.

“The complement of an Anti-decreasing (resp. an Anti-increasing) set is an Anti-increasing (resp. a Anti-decreasing) set. $C(A)$ denotes the complement of A in X .

$\text{Anti-icl}(A) = \bigcap \{F/F \text{ is an Anti-increasing closed subset of } X \text{ containing } A\}$

$\text{Anti-dcl}(A) = \bigcap \{F/F \text{ is a Anti-decreasing closed subset of } X \text{ containing } A\}$

$\text{Anti-bcl}(A) = \bigcap \{F/F \text{ is a closed subset of } X \text{ containing } A \text{ with } F = i(F) = d(F)\}$

$\text{Anti-IO}(X)$ (resp. $\text{Anti-DO}(X)$, $\text{Anti-BO}(X)$) denotes the collection of all Anti-increasing (resp. Anti-decreasing, both Anti-increasing and Anti-decreasing) open subsets of an Anti-topological ordered space (X, τ, \leq) . For a subset A of a space (X, τ, \leq) , $\text{Anti-icl}(A)$ (resp. $\text{Anti-dcl}(A)$, $\text{Anti-bcl}(A)$) denote the Anti-increasing (resp. Anti-decreasing, both Anti-increasing and Anti-decreasing) closure of A ”.

Definition 5.4: If $\text{Anti-icl}(A) \subseteq U$ every time “ $A \in U$ ”, where U is Anti-O then A is an Anti-ig-cs.

Definition 5.5: If $\text{Anti-dcl}(A) \subseteq U$ every time “ $A \in U$ ”, where U is Anti-O then A is an Anti-dg-cs.

Definition 5.6: If $\text{Anti-bcl}(A) \subseteq U$ every time “ $A \in U$ ”, where U is Anti-O then A is an Anti-bg-cs

Theorem 5.7: Every Anti-bclosed set is an Anti-iclosed set.

Proof: W.k.t “Every balanced set is an increasing set”. Afterward every Anti-bclosed set is an Anti-iclosed.

Example 5.8: Let $X = \{1, 2, 3, 4, 5\}$, $\tau = \{\{1\}, \{4\}, \{2, 3\}, \{3, 5\}\}$ be an Anti-topology for X and $\leq = \{(1, 1), (2, 2), (3, 3), (2, 3), (3, 4)\}$. Let $P = \{1, 4, 5\}$. P is Anti-iclosed set rather than a Anti-bclosed set.

Theorem 5.9: Every Anti-bclosed set is an Anti-dclosed set.

Proof: W.k.t “Every balanced set is a decreasing set”. Afterward every Anti-bclosed set is a Anti-dclosed.

Example 5.10: Consider ex 5.8. Let $P = \{1, 2, 3, 5\}$. P is Anti-dclosed set rather than a Anti-bclosed set.

Theorem 5.11: The concepts of anti-iclosedness and anti-dclosedness exist separately. The following examples will show this.

Example 5.12: Consider ex 5.8. Let $P = \{1, 4, 5\}$. P is Anti-iclosed set rather than a Anti-dclosed set. Let $Q = \{1, 2, 3, 5\}$. Q is Anti-dclosed set rather than a Anti-iclosed set.

Theorem 5.13: Each set that's anti-bg-closed is also anti-ig-closed.

Proof: W.k.t “Every balanced set is an increasing set”. Afterward every Anti-bg-cs is an Anti-ig-cs.

Example 5.14: Consider ex 5.8. Let $P = \{4\}$. P is Anti-igclosed set rather than an Anti-bgclosed set.

Theorem 5.15: Every Anti-bg-cs is an Anti-dg-cs.

Proof: W.k.t “Every balanced set is a decreasing set”. Afterward every Anti-bg-cs is an Anti-dg-cs.

Example 5.16: Consider ex 5.8. Let $P = \{2\}$. P is Anti-dgclosed set rather than a Anti-bgclosed set.

Theorem 5.17: Anti-dg and Anti-ig closedness are two different concepts. The following examples will show this.

Example 5.18: Consider ex 5.8. Let $P = \{4\}$. P is Anti-igclosed set rather than a Anti-dgclosed set. Let $Q = \{2\}$. Q is Anti-dgclosed set rather than a Anti-igclosed set.

Theorem 5.19: “If there isn't a non-empty Anti-iclosed set in $\text{Anti-icl}(A)$ - A iff set A is Anti-ig-closed.

Proof: Suppose F is an Anti-c portion of $\text{Anti-icl}(A)$ - A . If $A \subseteq C(F)$ & since A is Anti-ig-c, we get $\text{Anti-icl}(A) \subseteq C(F)$ or $F \subseteq C(\text{Anti-icl}(A))$. Thus $F \subseteq \text{Anti-icl}(A) \cap C(\text{Anti-icl}(A)) = \emptyset \Rightarrow F = \emptyset$.

Conversely suppose that $A \subseteq O$ & that O is anti-open. If $\text{Anti-icl}(A)$ does not contained O , then $\text{Anti-icl}(A)$ - A has a not void Anti-c portion called $\text{anti-icl}(A) \cap C(O)$ ”.

Theorem 5.20: “ $A \cap B$ ” is anti-ig-c if A, B are both anti-ig-c.

Proof: If $A \cap B \subseteq O$ & O is Anti-open, $\text{Anti-icl}(A) \subseteq O$ and $\text{Anti-icl}(B) \subseteq O$. $\text{Anti-icl}(A) \cap \text{Anti-icl}(B) \subseteq O \cap O = O \Rightarrow \text{Anti-icl}(A) \cap \text{Anti-icl}(B) \subseteq O$ (1)

W.k.t “ $\text{Anti-icl}(A \cap B) \subseteq \text{Anti-icl}(A) \cap \text{Anti-icl}(B)$ ” (2)

From (1) and (2), we have “ $\text{Anti-icl}(A \cap B) \subseteq \text{Anti-icl}(A) \cap \text{Anti-icl}(B) \subseteq O$ ”

Anti-icl($A \cap B$) $\subseteq O$

Therefore Anti-icl($A \cap B$) $\subseteq O$ whenever $A \cap B \subseteq O$ and O is Anti-open.

Hence $A \cap B$ is Anti-ig-closed.

Theorem 5.21: If B is an anti-ig-closed set with respect to A and A is an anti-ig-c portion of X , next B is also anti-ig-c in X .

Proof: Let $B \subseteq O$ & O be Anti-o in $X \Rightarrow "B \subseteq A \cap O"$ & hence $Anti-icl_A(B) = A \cap O$. That means that $A \cap Anti-icl(B) \subseteq A \cap O$ and $A \subseteq O \cup C(Anti-icl(B))$. X is Anti-ig-closed for A , therefore $Anti-icl(A) \subseteq O \cup C(Anti-icl(B))$. $Anti-icl(B) \subseteq Anti-icl(A) \subseteq O \cup C(Anti-icl(B))$ and $Anti-icl(B) \subseteq O$.

Theorem 5.22: If A is Anti-ig-c and $A \subseteq B \subseteq Anti-icl(A)$, then B is Anti-ig-c.

Proof: $Anti-icl(B) \cap B \subseteq Anti-icl(A) \cap A$ & void Anti-c portions exist in $Anti-icl(A) \cap A$ or $Anti-icl(B) \cap B$, thus use the known theorem.

Theorem 5.23: Given " $A \subseteq Y \subseteq X$ ", A is anti-ig-c in X . Anti-ig-closed A is related to Y .

Proof: Let $A \subseteq Y \cap O$ & presume that O is Anti-o in X . Then " $A \subseteq O$ & $Anti-icl(A) \subseteq O$ ". That means $Y \cap Anti-icl(A) \subseteq Y \cap O$.

Conclusion:

In this article, we have introduced the notion of Anti-g-css and Anti-g-css in connection with ATS and Anti-ig-closed, Anti-dg-closed and Anti-bg-css in ATOS and then explored their fundamental properties. Furthermore, we have defined the Anti-g*-c & Anti-g*-open of a set, delving into an in-depth analysis of their associated properties. From the above discussion, we have found that classes of anti-g-oss and anti-g-css in anti-topological spaces are finer than classes of anti-oss & anti-css, respectively. Also, the deviations from standard topological expectations signify the unique characteristics of the anti-topological space under consideration.

As we move forward, our future research endeavors will aim to investigate novel concepts and ideas related to anti-topological spaces. We anticipate that the insights presented in this article will contribute to the advancement of various facets within the field of anti-topological spaces,

aiding researchers in their exploration and development of this intriguing domain.

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